2

SUPERVISOR'S USE ONLY

91262



## Level 2 Mathematics and Statistics, 2016 91262 Apply calculus methods in solving problems

9.30 a.m. Thursday 24 November 2016 Credits: Five

Achievement	Achievement with Merit	Achievement with Excellence
Apply calculus methods in solving problems.	Apply calculus methods, using relational thinking, in solving problems.	Apply calculus methods, using extended abstract thinking, in solving problems.

Check that the National Student Number (NSN) on your admission slip is the same as the number at the top of this page.

## You should attempt ALL the questions in this booklet.

Make sure that you have Formulae Sheet L2-MATHF.

Show ALL working.

If you need more space for any answer, use the page(s) provided at the back of this booklet and clearly number the question.

You must show the use of calculus in answering all questions in this paper.

Check that this booklet has pages 2–12 in the correct order and that none of these pages is blank.

YOU MUST HAND THIS BOOKLET TO THE SUPERVISOR AT THE END OF THE EXAMINATION.

TOTAL

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(a) A function *f* is given by  $f(x) = 4x^3 - 7x^2 + 2x - 4$ .

Find the gradient of the graph of the function at the point where x = 2.

(b) The line y = x + 3.25 is a tangent to the graph of the function  $f(x) = 3x^2 - 2x + 4$ .

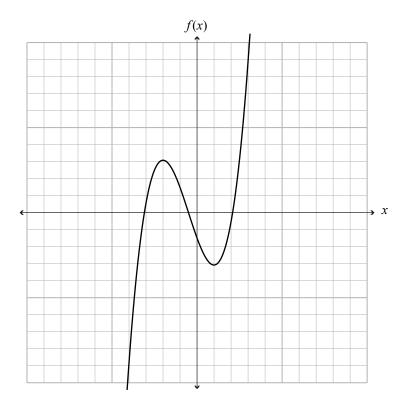
Use calculus to show that the line is a tangent to the curve, and that the point where this tangent touches the curve is (0.5,3.75).

(c) The function  $f(x) = 2x^3 + kx^2 + 5$  has a minimum turning point when x = 1.

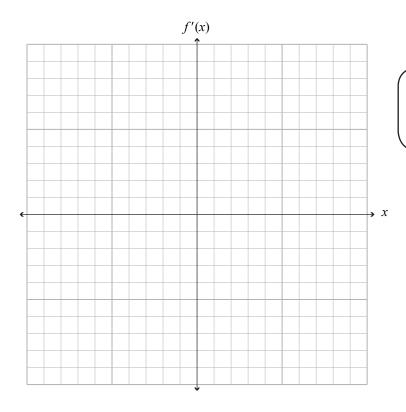
What are the coordinates of the **maximum** turning point?

The equation a constant.	or a ranction y				
The point $(3,$	4) is the turning p	oint on the graph of	f the function.		
Find the equa	ation of the functi	on.			
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		of the function $y = y$	$x^{3}(x-4)$ .		-
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The diagram below shows the graph of the function y = f(x). (a)



On the axes below sketch the gradient function y = f'(x).



If you need to redraw this graph, use the grid on page 11.

## This question has been corrected from that used in the examination.

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Find	I the values of $a$ and $b$ .
A fo	nction f is given by $f(x) = 2 - 4x + 5x^2 + ax^3$ .
	gradient of the graph of the function at the point where $x = 1$ is 3.
1116	gradient of the graph of the function at the point where $x = 1$ is 3.
Find	the value of a.

(d)	A chemical is slowly leaking onto a floor.	ASSESSOR'				
	The chemical spreads out from the point where it lands in a shape that can be modelled by a circle of radius $r$ cm.					
	At a time $t$ seconds after the chemical leak is noticed, $r$ is given by $0.1t + 2$ .					
	Use calculus to find the rate of change of area of the circle, with respect to time, when its radius is 10 cm.					
	(Area of circle = $\pi r^2$ )					
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(e)	A function is defined by $y = 3x^3 - 4a^2x + 5$ where a is a positive number.					
	Find the range of values of $x$ in terms of $a$ for which the function is decreasing.					
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## **QUESTION THREE**

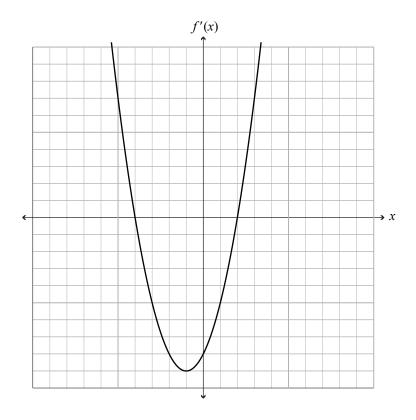
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(a) The gradient function for a curve is given by  $\frac{dy}{dx} = 3x^2 - 5$ . The curve passes through the point (1,0).

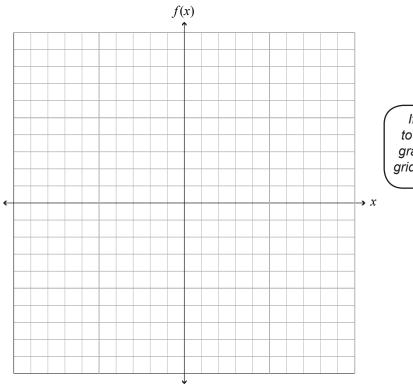
Find the equation of the curve

(b) The diagram below shows the graph of the gradient function y = f'(x) of a function y = f(x).

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On the axes below sketch the graph of the function y = f(x).



If you need to redraw this graph, use the grid on page 11.

(c)	Meg is riding her motocross bike.					
	When she passes a fixed point P on the track, she has a speed, $v$ , of 5 m s <sup>-1</sup> , and her acceleration, $a$ , is 0.6 m s <sup>-2</sup> .					
	(i)	If she were to continue to accelerate at this rate, what is her speed when she has been riding for 10 seconds after passing P?				
	(ii)	How far will she have travelled from P when she reaches a speed of 8 m s <sup>-1</sup> ?				

**Question Three continues on the following page.** 

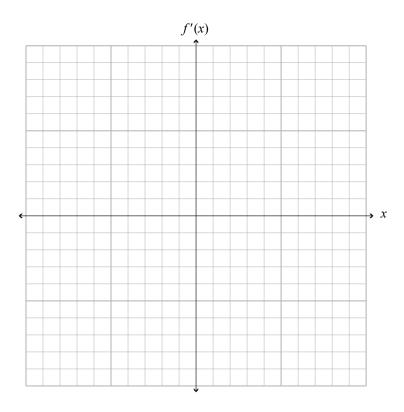
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f he decelerates at 0.2 m s	<sup>2</sup> , how far past the point	t P will he be when he reache	s a
speed of 6 m s <sup>-1</sup> ?			

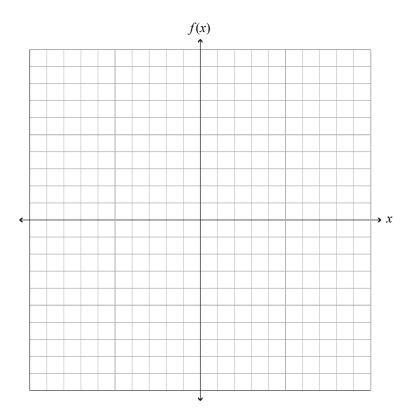
SPARE GRIDS

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If you need to redraw your graph from Question Two (a), draw it on the grid below. Make sure it is clear which answer you want marked.



If you need to redraw your graph from Question Three (b), draw it on the grid below. Make sure it is clear which answer you want marked.



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	Extra paper if required.	
1	Write the question number(s) if applicable.	
QUESTION NUMBER	write the question number(s) if applicable.	