2

SUPERVISOR'S USE ONLY

91262



Level 2 Mathematics and Statistics, 2018 91262 Apply calculus methods in solving problems

9.30 a.m. Wednesday 14 November 2018 Credits: Five

Achievement	Achievement with Merit	Achievement with Excellence
Apply calculus methods in solving problems.	Apply calculus methods, using relational thinking, in solving problems.	Apply calculus methods, using extended abstract thinking, in solving problems.

Check that the National Student Number (NSN) on your admission slip is the same as the number at the top of this page.

You should attempt ALL the questions in this booklet.

Make sure that you have Formulae Sheet L2-MATHF.

Show ALL working.

If you need more space for any answer, use the page(s) provided at the back of this booklet and clearly number the question.

You must show the use of calculus in answering all questions in this paper.

Check that this booklet has pages 2–15 in the correct order and that none of these pages is blank.

YOU MUST HAND THIS BOOKLET TO THE SUPERVISOR AT THE END OF THE EXAMINATION.

TOTAL

QUESTION ONE

ASSESSOR'S USE ONLY

(a) A function f is given by $f(x) = x^3 - 6x + 2$.

Find the gradient of the graph of the function at the point where x = 4.

(b) A rectangle is expanding in area so that at all times its length is three times its width.

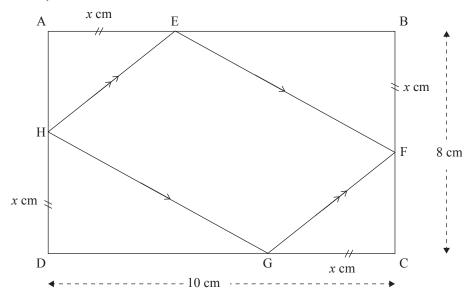
Find the rate of change of the area of the rectangle with respect to its width when the area of the rectangle is 75 cm².

	e derivative of a function f is given by $f'(x) = -3x^2 + 12x$. e graph of the function has a local minimum at the point $(0,5)$.	AS L
	e calculus to find the value of the local maximum of the function.	
Us	e calculus to find the values of x for which the graph of the function	
Use	the calculus to find the values of x for which the graph of the function $(x) = \frac{2}{3}x^3 + \frac{9}{2}x^2 - 5x - 18$ is increasing.	
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(e) A rectangle ABCD measures 10 cm by 8 cm. A parallelogram EFGH can be drawn inside the rectangle, as shown in the diagram below.

Suppose that the distance from each corner of the rectangle to the next vertex of the parallelogram, in a clockwise direction, is x cm.

That is, AE = BF = CG = DH = x.



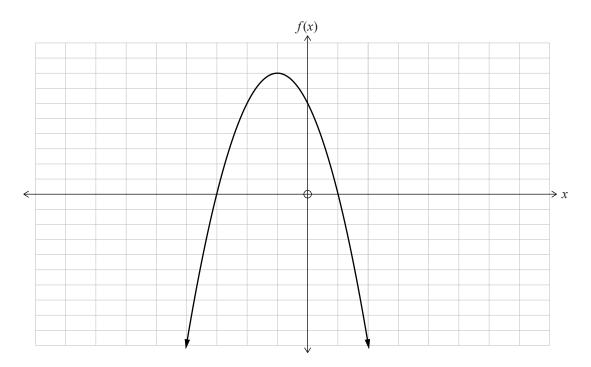
Use calculus to find the smallest possible area that the parallelogram can have.

Justify that your ans	wer is a minimum.		

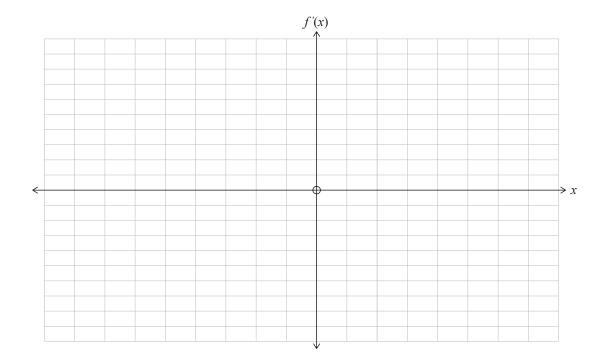
QUESTION TWO

ASSESSOR'S USE ONLY

(a) The graph of a function y = f(x) is shown on the axes below.



Sketch the graph of the gradient function y = f'(x) on the axes below. Both sets of axes have the same scale.

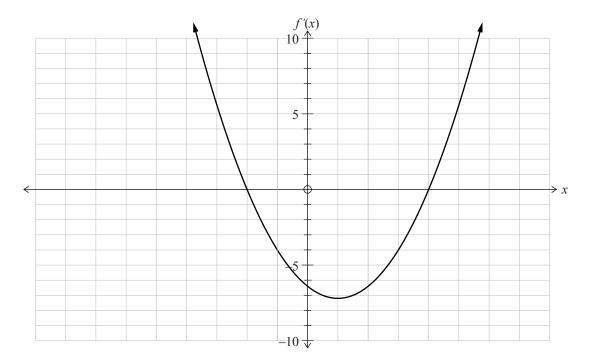


If you need to redo this question part, use the grids on page 12.

A skyrocket is projected into the air so that <i>t</i> seconds after it is launched, its height, <i>h</i> metres, above the ground is given by	AS U
$h(t) = 39.2t - 4.9t^2.$	
What is the maximum height that the skyrocket will reach?	
Adam is operating his drone. It is moving in a straight line and t seconds after passing a tree its acceleration, $a \text{ m s}^{-2}$, is given by	
a(t) = 6 - 12t.	
Two seconds after the drone passed the tree, its velocity was 20 m s ⁻¹ .	
How far was the drone from the tree when its velocity was 20 m s ⁻¹ ?	
	-

(d) The diagram below shows the graph of the gradient function y = f'(x) of a function y = f(x).

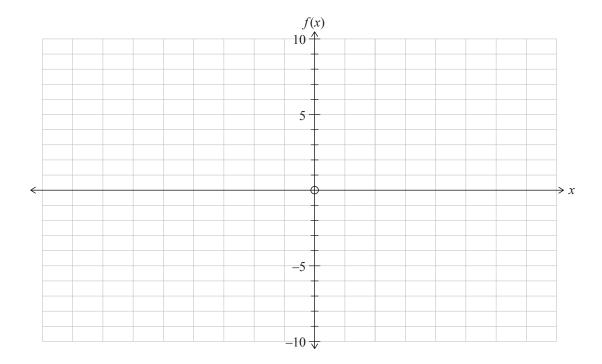




The graph of the function y = f(x) passes through (0,3).

On the axes below sketch the graph of the function *f*.

Both sets of axes have the same scale.



If you need to redo this question part, use the grids on page 13.

Determine the nature of	f each turning point, justifying your answer.	
	reach turning point, justifying your unswer.	

QUESTION THREE

ASSESSOR'S	
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The gradient function of a curve is given by $\frac{dy}{dx} = -5x^4 + 6$.
The curve passes through (1,7).
Find the equation for <i>y</i> .
Suppose that at the start of a particular day 1000 mapple grows trading in a market and that
Suppose that, at the start of a particular day, 1000 people were trading in a market, and that days after the start of that day, the number of traders, N , can be modelled by
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days after the start of that day, the number of traders, N , can be modelled by $N(t) = 1000 + 400t + 100t^2.$ How many days will it take for the rate of change of the number of traders to be 14400 per
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Question Three continues on the following page.

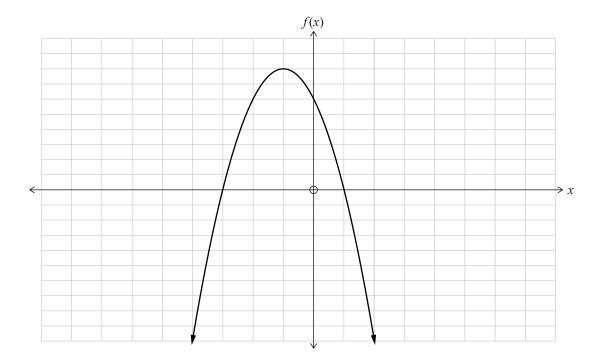
A school is selling tickets for its drama production. The revenue, R , from selling tickets for a price of p each, can be modelled by the full $R(p) = 40p(29 - 2p)$	nction
Use calculus to find the maximum possible revenue (using this model).	

at a certain point P, has grad	ient of –7 and intersects the gra	pii agaiii at (-0,04).	
Use calculus to find the co-c	ordinates of the point P.		
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If you need to redo Question Two (a), use the grid below. Make sure it is clear which answer you want marked.

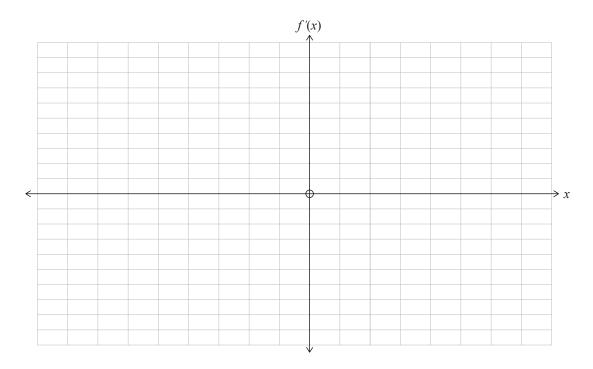
QUESTION TWO

(a) The graph of a function y = f(x) is shown on the axes below.



Sketch the graph of the gradient function y = f'(x) on the axes below.

Both sets of axes have the same scale.

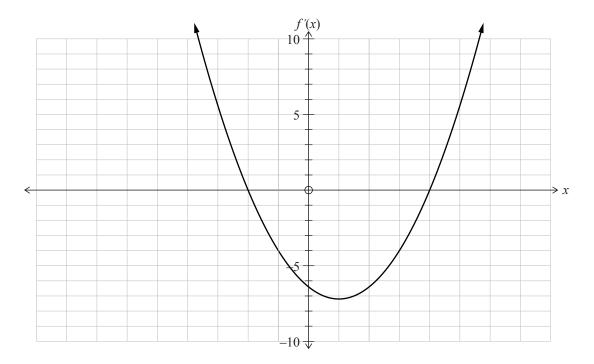


If you need to redo Question Two (d), use the grid below. Make sure it is clear which answer you want marked.

ASSESSOR'S USE ONLY

QUESTION TWO

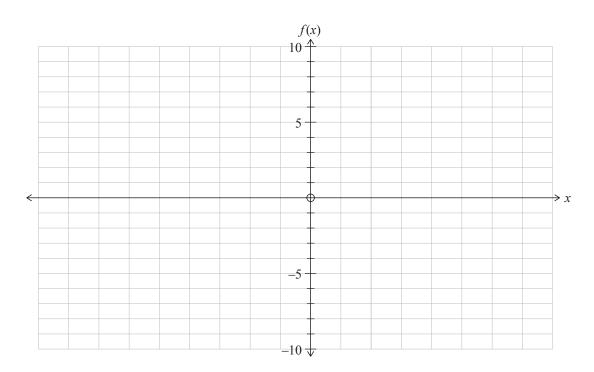
(d) The diagram below shows the graph of the gradient function y = f'(x) of a function y = f(x).



The graph of the function y = f(x) passes through (0,3).

On the axes below sketch the graph of the function f.

Both sets of axes have the same scale.



	Extra space if required.	ASSESSOR'	S
QUESTION NUMBER	Write the question number(s) if applicable.	USE ONLY	
NUMBER			

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