## Assessment Schedule – 2014

# Physics: Demonstrate understanding of mechanical systems (91524)

#### Assessment Criteria

| Achievement   | Achievement with Merit                                     | Achievement with Excellence                              |
|---|--|--|
| <i>Demonstrate understanding</i> requires writing statements that | <i>Demonstrate in-depth understanding</i> requires writing | <i>Demonstrate comprehensive understanding</i> requires  |
| typically show an awareness of how simple facets of               | statements that typically give reasons why phenomena,      | writing statements that typically give reasons why       |
| phenomena, concepts or principles relate to a described           | concepts or principles relate to given situations. For     | phenomena, concepts or principles relate to given        |
| situation. For mathematical solutions, relevant concepts will be  | mathematical solutions, the information may not be         | situations. Statements will demonstrate understanding of |
| transparent, methods will be straightforward.                     | directly useable or immediately obvious.                   | connections between concepts.                            |

#### **Evidence Statement**

| Q                    | Evidence  | Achievement   | Merit  | Excellence |
|----------------------|---|---|--|------------|
| <b>ONE</b><br>(a)(i) | $\omega = \frac{\Delta\theta}{\Delta t} \qquad T = \frac{360^{\circ}}{\omega} = \frac{360^{\circ}}{14.7} = 24.49 \text{ days}$<br>= 24.49 × 24 × 60 × 60 = 2.11 × 10 <sup>6</sup> s | • $\frac{360}{14.7} = 24.5 \text{ days}$<br>OR<br>Correct $\omega$ : = 1.7014 × 10 <sup>-4</sup> ° s <sup>-1</sup> OR<br>$\omega = 2.96 \times 10^{-6} \text{ rad s}^{-1}$ (written with<br>$\omega$ or with units<br>OR<br>$\frac{360}{14.7} \times 86400$ (shows subs but not<br>equation)<br>• Correct working showing conversion of<br>days to seconds. | • Correct working showing conversion<br>of days to seconds.<br>AND<br>Uses $\omega = \frac{\Delta \theta}{\Delta t}$ OR<br>$T = \frac{1}{f}$ + proportional circle OR<br>$T = \frac{360/2\pi}{\omega}$<br>OR<br>Has described meaning of intermediate<br>step, eg:<br>24.48 days for full rotation<br>Or $1.7 \times 10^{-40}$ s <sup>-1</sup><br>Or $2.96 \times 10^{-6}$ rad s <sup>-1</sup><br>Or show ratios, eg14.7 day<br>$360 \Rightarrow 24.4$<br>Or $f = 4.73 \times 10^{-8}$ Hz)<br>Can go backwards, but has to be clear. |            |
| (a)(ii)              | $v = \frac{2\pi r}{T} = \frac{2 \times \pi \times 6.96 \times 10^8}{2.12 \times 10^6} = 2.066.7$<br>= 2070 m s <sup>-1</sup><br>(Answer: 2060 - 2070 dependent on rounding.)        | • Uses $v = \omega r$ with incorrect $\omega$ or $T$ and<br>correct $r$ .<br>OR<br>Uses $v = \frac{2\pi r}{T}$ with incorrect $T$ and<br>correct $r$ .<br>OR<br>Correct answer.<br>OR<br>Correct subs with wrong answer.  | • Correct speed 2060 – 2070 m s <sup>-1</sup><br>with some working – (subs or eqn).  |            |

| (b) | When the core of the Sun collapses, this will cause<br>the radius of the particles in the core to rotate with a<br>smaller radius. Angular momentum will be<br>conserved, so if the rotational inertia decreases, the<br>core will have to rotate at a higher angular velocity.   | <ul> <li>Angular momentum is conserved.</li> <li>Rotational inertia of core will get<br/>smaller.</li> <li>OR<br/>Angular velocity increases because mass<br/>is closer to the centre / axis.</li> <li>Accept inertia in place of rotational<br/>inertia.</li> </ul> | <ul> <li>Angular momentum is conserved, therefore if rotational inertia decreases, angular velocity increases OR <ul> <li><i>L</i> = <i>I</i>ω therefore, if <i>I</i> decreases, ω increases.</li> </ul> </li> <li>OR <ul> <li>ω increases because <i>I</i> decreases due to mass closer to the centre / axis.</li> </ul> </li> <li><i>Accept inertia in place of rotational inertia.</i></li> <li><i>Radius smaller is acceptable for mass closer to the centre / axis.</i></li> </ul> | <ul> <li>Angular momentum is<br/>conserved AND L = Iω<br/>AND<br/>I decreases due to mass closer<br/>to the centre / axis<br/>THEREFORE ω increases.</li> <li>Accept inertia in place of<br/>rotational inertia.<br/>radius smaller is acceptable for<br/>mass closer to the centre / axis.</li> </ul> |
|-----|---|--|---|--|
| (c) | For geostationary motion, the period of the satelite<br>has to be equal to the period of Mercury<br>And $F_c = F_g$<br>$\frac{GMm}{r^2} = \frac{mv^2}{r} \qquad v = \frac{2\pi r}{T}$ $r^3 = \frac{GMT^2}{4\pi^2}$ $r = \sqrt[3]{\frac{6.67 \times 10^{-11} \times 3.30 \times 10^{23} \times (5.067 \times 10^6)^2}{4\pi^2}}$ $r = 2.43 \times 10^8 \text{ m}$ | • $F_{c} = F_{g}$<br>OR<br>$\frac{mv^{2}}{r} = \frac{GMm}{r^{2}}$<br>OR<br>$v = \sqrt{\frac{GM}{r}}$<br>• $v = \frac{2\pi r}{T}$<br>• Period of satelite period of Mercury<br><i>MAXIMUM 2As</i>   | Merges $(F_c = F_g OR \ \frac{mv^2}{r} = \frac{GMm}{r^2})$<br>• And<br>$v = \frac{2\pi r}{T}$ , or $v = \omega r$ , $\omega = 2\pi f$<br>with rearranging incorrect<br>OR<br>Using $F_c = F_g$ to derive $r = \frac{GM}{v^2}$<br>OR<br>Full answer going backwards.   | Correct rearrangement and<br>substitution for $r^3$ or cube root<br>of $r$<br>AND<br>$(F_c = F_g OR \frac{mr^3}{r} = \frac{GMm}{r^3})$<br>AND $v = \frac{2\pi r}{T}$   |

| The m<br>so the<br>decrea<br>will al<br>will be<br>remain<br><u>Interp</u><br>Angul<br>extern<br>same. | erpreted as if Total probe:<br>e mass that is lost will have angular momentum,<br>the angular momentum of the space probe will<br>rease. The rotational inertia of the space probe<br>l also decrease. The effect of these two changes<br>l be that they cancel and the angular velocity will<br>nain constant.<br>erpreted as if Partial probe:<br>gular momentum is conserved because of no<br>ernal torque, therefore angular speed stays the<br>ne. / Instrument does not apply torque to the rest<br>he probe ,so angular speed does not change. | • TOTAL probe: Loss of instrument<br>means decrease in rotational inertia or<br>angular momentum of probe<br>OR<br>PARTIAL probe: No torques therefore<br>angular speed stays the same.<br>OR<br>MISINTERPRETATION: Idea that<br>orbital speed is independent of mass of<br>satellite. Has to show idea of mass<br>cancelling from $F_c$ or $F_g$ or not in<br>$v = \sqrt{\frac{GM}{r}}$ | • TOTAL probe: instrument takes <i>L</i> away and <i>I</i> away, therefore angular speed stays the same. $L = I\omega$<br>OR<br>PARTIAL probe: instrument does not apply torque to the rest of the probe does not change angular speed. |  |
|--|---|--|---|--|
|--|---|--|---|--|

| Q1 | Not Achieved                            |    | Not Achieved Achievement Achiev |    | Achieveme | nt with Merit | Achievement with Excellence |         |         |
|----|---|----|---------------------------------|----|-----------|---------------|-----------------------------|---------|---------|
|    | NO                                      | N1 | N2                              | A3 | A4        | M5            | M6                          | E7      | E8      |
|    | No response,<br>no relevant<br>evidence | 1A | 2A                              | 3A | 4A        | 2M + 1A       | 3M<br>Or<br>1E + 1M         | 1E + 2M | 2E + 1M |

| TWO<br>(a) | $T = 2\pi \sqrt{\frac{l}{g}} = 2\pi \sqrt{\frac{1.55}{9.81}} = 2.50 \text{ s}$ $t = \frac{1}{2}T = 1.25 \text{ s}$   | • Correct period.  |  |  |
|------------|--|--|--|--|
| (b)        | Tension and gravitational force add to make the restoring force towards the equilibrium.<br>$F_{T}$ $F_{g}$ $F_{g}$ The bob is stationary at point of release. This restoring force makes the bob speed up from as it goes towards the middle.<br>The restoring force decreases and goes to zero as the bob goes to the middle, so the acceleration decreases to zero and the bob has constant speed at the equilibrium position.<br>Accept $F_{res}$ horizontal | <ul> <li>Gravitational and tension forces identified.</li> <li>Force is towards the equilibrium position.<br/>OR<br/>Force proportional to displacement<br/>OR<br/>At equilibrium no force AND at end points maximum force.</li> <li>At release point v = 0, and at equilibrium v is maximum.<br/>OR<br/>Speeds up / accelerates as it goes towards the centre.</li> <li>MAXIMUM 2As<br/>Accept net /total / restoring force in place of force, but not gravitational force or tension force.</li> </ul> | <ul> <li>F<sub>T</sub></li> <li>F<sub>g</sub></li> <li>OR</li> <li>Idea of direction of tension and gravitational force (either stating the directions or saying they don't cancel, or correct ideas of components)</li> <li>OR</li> <li>(<i>F</i><sub>res</sub> towards equilibrium SO that bob speeds up / accelerates. AND</li> <li>Restoring force decreases so acceleration decreases OR At equilibrium no F<sub>res</sub> so constant speed / no acceleration.)</li> <li>Accept net force /total force in place of restoring force.</li> </ul> | • (<br>• (<br>$F_T$<br>$F_g$<br>$F_g$<br>$F_{Res}$<br>OR<br>Idea of direction of tension<br>and gravitational force (either<br>stating the directions or saying<br>they don't cancel, or correct<br>ideas of components).)<br>AND<br>$F_{res}$ towards equilibrium SO<br>that bob speeds up /<br>accelerates.<br>AND<br>Restoring force decreases so<br>acceleration decreases OR At<br>equilibrium no $F_{res}$ , so<br>constant speed/no<br>acceleration.<br>Accept net force /total force in<br>place of restoring force. |

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| (c)(i) | $r = 0.290 \text{ m} \qquad L = 1.55 \text{ m}$ $\sin \theta = \frac{r}{L} = \frac{0.290}{1.55} \qquad F_{\text{T}} \qquad \theta \qquad \text{mg}$ $\Rightarrow \theta = 10.78^{\circ} \text{ or } 0.188 \text{ rad}$ $F_{\text{g}} = mg \qquad F_{\text{c}} \qquad F_{\text{c}} \qquad F_{\text{c}} \qquad \theta \qquad F_{\text{c}}$ $= 1.8 \times 9.81 \qquad F_{\text{c}} \qquad F_{\text{c}} \qquad F_{\text{c}} \qquad \theta \qquad F_{\text{c}} \qquad \theta \qquad F_{\text{c}} \qquad \theta \qquad$   | • Correct angle<br>OR<br>Find $F_g = 17.658$ and use INCORRECT<br>angle to find $F_T$  | • Correct tension force showing<br>working for correct angle.<br>AND evidence of correct trig used.<br>$F_{\rm T} = \frac{F_{\rm g}}{\cos\theta}$<br>AND $F_{\rm g} = 17.658$ or evidence of<br>mg used.   |   |
|--------|---|--|--|---|
|        | ALERT: $\theta$ $\tan^{-1}\left(\frac{0.20}{1.55}\right)$ 10.50 is wrong answer<br>$\cos\theta = \frac{F_{\rm C}}{F_{\rm T}} = \frac{0.290}{1.55}$<br>$\Rightarrow F_{\rm C} = \frac{0.290 \times 17.975}{1.55} = 3.3631$<br>$F_{\rm C} = \frac{mv^2}{r} \Rightarrow v = \sqrt{\frac{3.3631 \times 0.290}{1.8}} = 0.7361$<br>$v = 0.74 {\rm ms^{-1}}$<br>$F_{\rm T}$<br>$H_{\rm T}$<br>$H_{\rm C}$<br>$H_{\rm C}$<br>$\Rightarrow$<br>$H_{\rm C}$<br>$H_{\rm C}$<br>$H_$ | • Obtain $F_c$ as number or equation<br>Eg $F_c = F_g \tan \theta$<br>or $F_c = F_T \sin \theta$<br>or $F_c = \sqrt{F_T^2 - F_g^2}$<br>OR<br>Uses $F_c = \frac{mv^2}{r}$ to find <i>v</i> with wrong <i>F</i> .<br>Follow on error accepted. | • (Evidence of use of trig or<br>pythagorus in attempt to get $F_c$<br>AND uses $F_c = \frac{mv^2}{r}$ t o find $v$<br>(Eg mistakes – doesn't use sqr root,<br>uses wrong trig or sin in<br>pythagorus, or re-arrange<br>incorrectly))<br>OR<br>• Correct answer with insufficient<br>working<br>Follow on error accepted. | • Some working shown<br>$(F_c = \frac{mv^2}{r}$ plus correct trig or<br>pyth) and consistent answer and<br>unit.<br>Follow on error accepted. |

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| Q2 | Not Achieved                            |    | Not Achieved Achievement |    | Achievement with Merit |                   | Achievement with Excellence |         |        |
|----|---|----|--------------------------|----|------------------------|-------------------|-----------------------------|---------|--------|
|    | NO                                      | N1 | N2                       | A3 | A4                     | M5                | M6                          | E7      | E8     |
|    | No response,<br>no relevant<br>evidence | 1A | 2A                       | 3A | 4A                     | 2M<br>OR<br>1E+2A | 3M                          | 1E + 2M | 2E +1A |

| THREE<br>(a) | $p_{\text{system}} = (m_{\text{A}} + m_{\text{B}}) \times v_{\text{com}} = (0.517 + 0.684) \times v_{\text{com}}$ $p_{\text{system}} = p_{\text{A}} + p_{\text{B}} = 0.517 \times 1.21 + 0 = 0.62557$ $v_{\text{com}} = \frac{1.21 \times 0.517}{0.517 + 0.6841} = 0.52087 = 0.521 \text{ m s}^{-1}$ $= 0.521 \text{ m s}^{-1}$ | • $P = mv = 0.62557$<br>OR<br>evidence of correct number<br>calculated eg<br>$\frac{5.17 \times 1.21}{0.517 + 0.684} = 0.52087$  | • $p = mv$<br>OR<br>$m_1v_1 + m_2v_2 =$<br>$(m_1 + m_2)v_{COM}$<br>OR<br>$p_{COM \text{ or TOTAL}} = p_A + p_B$<br>AND<br>Substitution into equation to<br>find correct answer.  |   |
|--------------|---|--|--|---|
| (b)(i)       | Momentum is conserved, so the size of the change of momentum<br>on disc A is equal to the size of the change in momentum of disc<br>B. As B had no momentum to start with, its final momentum must<br>be equal to the change in momentum.<br>$\Delta p = mv \Rightarrow v = \frac{0.250}{0.684} = 0.365 \text{ m s}^{-1}$       | • Momentum is conserved.<br>OR<br>$\Delta p_{\rm B} = \Delta p_{\rm A}$ (In words, or<br>equations, or by stating<br>$\Delta p_{\rm B} = 0.250$ )<br>OR<br>Statement of Newton 3rd law,<br>$\Delta p = F\Delta t$<br>OR<br>$p = mv$ and $\frac{0.250}{0.684} = 0.365497$ | • Momentum is conserved<br>OR<br>$\Delta p_{\rm B} = \Delta p_{\rm A}$ (In words, or<br>equations, or by stating<br>$\Delta p_{\rm B} = 0.250$ )<br>OR<br>Statement of Newton 3rd law,<br>$\Delta p = F\Delta t$<br>AND<br>$p = mv$ and $\frac{0.250}{0.684} = 0.365497$ |   |
| (b)(ii)      | $p_{\text{system}} = 0.62557 \text{ kg m s}^{-1}$ $p_{\text{system}} = p_{\text{A}} + p_{\text{B}}$ $0.25 \text{ kg m s}^{-1}$ $0.62557 \text{ kg m s}^{-1}$ $p_{\text{A}} = \sqrt{0.62557^{2} - 0.25^{2}} = 0.57344$ $= 0.573 \text{ kg m s}^{-1}$   | <ul> <li><i>p</i> = <i>mv</i> equation used correctly for some momentum.</li> <li>ONLY if no credit given for (a) or (b)(i).</li> </ul>  | <ul> <li>Shows Pythagorus with<br/>momentum, wrong answer.<br/>OR<br/>Correct vector diagram with<br/>labels or numbers - diagram<br/>either Δp or total p. (Arrows<br/>not needed) wrong answer.</li> </ul>   | <ul> <li>Shows evidence of Pythagorus<br/>or vector diagram.<br/>AND<br/>Correct answer.</li> <li><i>Carry on error from wrong p</i><br/><i>in 3a or 3b(i) OK.</i></li> </ul> |

| (c) | The only forces that will be acting on the discs will be tension<br>force in the cord. As this is an internal force acting within the<br>system, neither the momentum of the system nor the velocity of<br>the centre of mass of the system will change.<br>No friction therefore no external force acting on the system thus<br>momentum is conserved. | <ul> <li>No friction / frictionless.<br/>OR<br/>No external forces.</li> <li>Tension / force on string is an<br/>internal force.<br/>OR<br/>Forces due to cord oppose /<br/>cancel.</li> </ul> | <ul> <li>No friction, no external forces.<br/>OR<br/>No external forces because<br/>force due to string is internal.<br/>OR<br/>No external forces because<br/>string forces oppose / cancel<br/>each other.</li> </ul> | <ul> <li>No friction therefore no<br/>external forces therefore p is<br/>conserved<br/>AND<br/>Force of the string is internal.<br/>OR<br/>string forces oppose / cancel<br/>each other.</li> </ul> |
|-----|---|--|---|---|
|     |   | (Accept closed system in place of "no external forces".)   | (Accept closed system in place of "no external forces".)  | (Accept closed system in place of "no external forces")   |

| Q3 | Not Achieved                         |    |    | Achiev | vement | Achievemen            | nt with Merit       | Achievement | with Excellence |
|----|--------------------------------------|----|----|--------|--------|-----------------------|---------------------|-------------|-----------------|
|    | NO                                   | N1 | N2 | A3     | A4     | M5                    | M6                  | E7          | E8              |
|    | No response, no<br>relevant evidence | 1A | 2A | 3A     | 4A     | 2M +1A<br>OR<br>1E+2A | 3M<br>OR<br>1E + 1M | 1E+1M +1A   | 2E + 1A         |

### Cut Scores

|             | Not Achieved | Achievement | Achievement with Merit | Achievement with Excellence |
|-------------|--------------|-------------|------------------------|-----------------------------|
| Score range | 0 - 6        | 7 – 13      | 14 – 18                | 19 – 24                     |