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SUPERVISOR'S USE ONLY

91577



Level 3 Calculus, 2017

91577 Apply the algebra of complex numbers in solving problems

9.30 a.m. Thursday 23 November 2017 Credits: Five

Achievement	Achievement with Merit	Achievement with Excellence
Apply the algebra of complex numbers in solving problems.	Apply the algebra of complex numbers, using relational thinking, in solving problems.	Apply the algebra of complex numbers, using extended abstract thinking, in solving problems.

Check that the National Student Number (NSN) on your admission slip is the same as the number at the top of this page.

You should attempt ALL the questions in this booklet.

Show ALL working.

Make sure that you have the Formulae and Tables Booklet L3-CALCF.

If you need more space for any answer, use the page(s) provided at the back of this booklet and clearly number the question.

Check that this booklet has pages 2–12 in the correct order and that none of these pages is blank.

YOU MUST HAND THIS BOOKLET TO THE SUPERVISOR AT THE END OF THE EXAMINATION.

TOTAL

QUESTION ONE

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(a) If u = 2 + 3i and v = 1 - 4i, find $\bar{u} - 3v$, giving your solution in the form a + bi.

(b) Write $\frac{36}{5-\sqrt{7}}$ in the form $a+b\sqrt{7}$, where a and b are integers.

(c) Solve the following equation for x in terms of p:

$$p\sqrt{x-2} - 5\sqrt{x} = 0$$

Find the Cartesian equation of the locus described by $ z + 2 - 7i = 2 z - 10 + 2i $.	
Write your answer in the form $(x + A)^2 + (y + B)^2 = K$.	

QUESTION TWO

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nd the value of d.	
unlify as for as possible the symposium $\sqrt{2k}$ $(\sqrt{19k}, \sqrt{9k})$	
nplify, as far as possible, the expression $\sqrt{2k} \left(\sqrt{18k} - \sqrt{8k} \right)$.	
and w are complex numbers such that $z = -2 + 3i$ and $zw = 15 - 3i$.	
and an exact value of $arg(w)$.	

Find all possible val	1 : 7/1		

QUESTION THREE

(a)	If $u = p^3 \operatorname{cis} \frac{\pi}{3}$ and $v =$	$p \operatorname{cis} \frac{\pi}{8}$, write	$\frac{u}{v}$	in polar form
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(b)	Solve the equation	$x^2 - 6x + 14 = 0$
(0)	Solve the equation	$\lambda = 0\lambda + 14 = 0$.

Give your solution in	n the form	$a \pm \sqrt{b}i$,	where a	and b	are rational	numbers
•						

Find the value	es of A , B , and C .
Solve the eau	ation $\frac{8+x}{x} = \sqrt{3}$, writing your solution in the form $x = a + b\sqrt{3}$.

Question Three continues on the following page.

	er such that $z = \frac{a+bi}{a-bi}$, where a and b are real number	
Prove that $\frac{z^2 + 1}{2z} = \frac{a^2}{a^2}$	$\frac{-b^2}{2}$.	
$2z = a^2$	$+b^2$	

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	Extra paper if required. Write the question number(s) if applicable.	
QUESTION NUMBER	write the question number(s) if applicable.	