

91578



NEW ZEALAND QUALIFICATIONS AUTHORITY  
MANA TOHU MĀTAURANGA O AOTEAROA

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SUPERVISOR'S USE ONLY

## Level 3 Calculus, 2013

### 91578 Apply differentiation methods in solving problems

9.30 am Wednesday 13 November 2013

Credits: Six

Achievement	Achievement with Merit	Achievement with Excellence
Apply differentiation methods in solving problems.	Apply differentiation methods, using relational thinking, in solving problems.	Apply differentiation methods, using extended abstract thinking, in solving problems.

Check that the National Student Number (NSN) on your admission slip is the same as the number at the top of this page.

**You should attempt ALL the questions in this booklet.**

Show ALL working.

Make sure that you have the Formulae and Tables Booklet L3-CALCF.

If you need more space for any answer, use the page(s) provided at the back of this booklet and clearly number the question.

Check that this booklet has pages 2–12 in the correct order and that none of these pages is blank.

**YOU MUST HAND THIS BOOKLET TO THE SUPERVISOR AT THE END OF THE EXAMINATION.**

**TOTAL**

ASSESSOR'S USE ONLY

You are advised to spend 60 minutes answering the questions in this booklet.

**QUESTION ONE**

- (a) Differentiate  $y = \tan(x^2 + 1)$ .

*You do not need to simplify your answer.*

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- (b) Find the gradient of the tangent to the function  $f(x) = \ln(3x - e^x)$  at the point where  $x = 0$ .

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- (c) Find the  $x$  values of any points of inflection on the graph of the function  $y = e^{(6-x^2)}$ .

*Show any derivatives that you need to find when solving this problem.*

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## QUESTION TWO

(a) Differentiate  $y = \sqrt[3]{\pi - x^2}$ .

*You do not need to simplify your answer.*

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(b) A curve has the equation  $y = (x^3 - 2x)^3$ .

Find the equation of the tangent to the curve at the point where  $x = 1$ .

*Show any derivatives that you need to find when solving this problem.*

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(c) For what value of  $k$  does the function  $f(x) = x - e^x - \frac{k}{x}$  have a stationary point at  $x = -1$ ?

*Show any derivatives that you need to find when solving this problem.*

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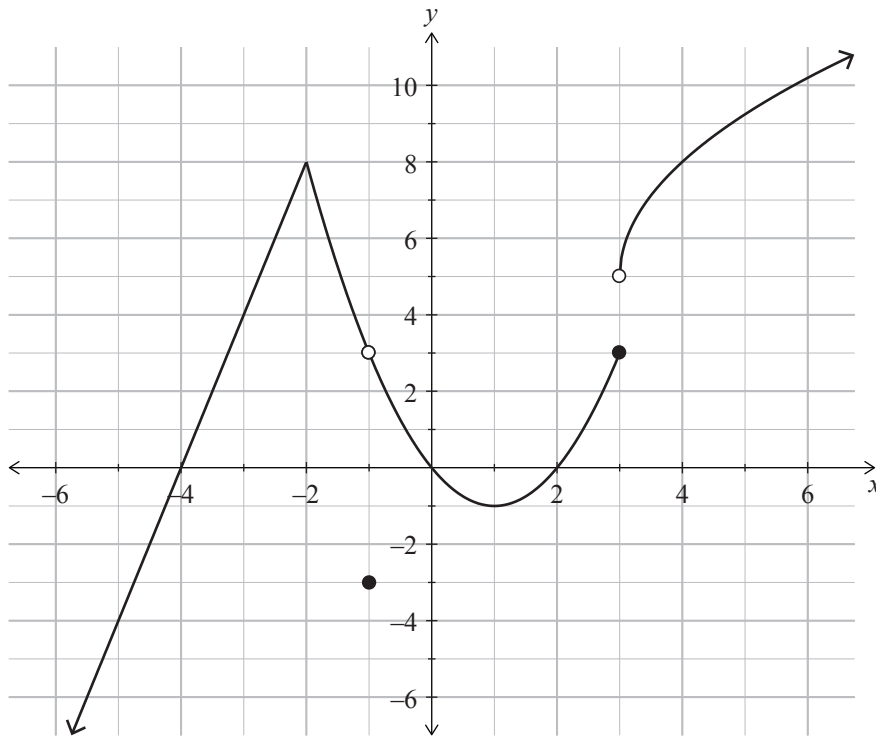
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(d) The graph below shows the function  $y = f(x)$ .



For the function  $f(x)$  above:

(i) Find all the value(s) of  $x$  that meet each of the following conditions:

1.  $f'(x) = 0$  \_\_\_\_\_
2.  $f''(x) < 0$  \_\_\_\_\_
3.  $f(x)$  is not differentiable \_\_\_\_\_

(ii) What is the value of  $f(-1)$ ? \_\_\_\_\_

(iii) What is the value of  $\lim_{x \rightarrow 3} f(x)$ ?

State clearly if the value does not exist.

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**QUESTION THREE**

(a) Differentiate  $y = \frac{\sin(2x)}{x^2}$ .

*You do not need to simplify your answer.*

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(b) For the function  $f(x) = x + \frac{16}{x-2}$ , find the  $x$ -values of any stationary points.

*You must use calculus and clearly show your working, including any derivatives you need to find when solving this problem.*

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