

SUPERVISOR'S USE ONLY

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91578



Draw a cross through the box (☒) if you have NOT written in this booklet

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Mana Tohu Mātauranga o Aotearoa  
New Zealand Qualifications Authority

## Level 3 Calculus 2023

### 91578 Apply differentiation methods in solving problems

Credits: Six

Achievement	Achievement with Merit	Achievement with Excellence
Apply differentiation methods in solving problems.	Apply differentiation methods, using relational thinking, in solving problems.	Apply differentiation methods, using extended abstract thinking, in solving problems.

Check that the National Student Number (NSN) on your admission slip is the same as the number at the top of this page.

**You should attempt ALL the questions in this booklet.**

Make sure that you have the Formulae and Tables Booklet L3–CALCF.

Show ALL working.

If you need more room for any answer, use the extra space provided at the back of this booklet.

Check that this booklet has pages 2–16 in the correct order and that none of these pages is blank.

Do not write in any cross-hatched area (DO NOT WRITE). This area will be cut off when the booklet is marked.

**YOU MUST HAND THIS BOOKLET TO THE SUPERVISOR AT THE END OF THE EXAMINATION.**

## QUESTION ONE

(a) Differentiate  $y = \sqrt{3x-2}$ .

*You do not need to simplify your answer.*

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(b) Find the rate of change of the function  $f(t) = t^2 e^{2t}$  when  $t = 1.5$ .

*You must use calculus and show any derivatives that you need to find when solving this problem.*

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## QUESTION TWO

(a) Differentiate  $f(x) = \frac{x^2}{\cos x}$ .

*You do not need to simplify your answer.*

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(b) Find the gradient of the tangent to the curve  $y = \cot(2x)$  at the point where  $x = \frac{\pi}{12}$ .

*You must use calculus and show any derivatives that you need to find when solving this problem.*

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### QUESTION THREE

- (a) Differentiate  $y = \ln(x^2 - x^4 + 1)$ .

*You do not need to simplify your answer.*

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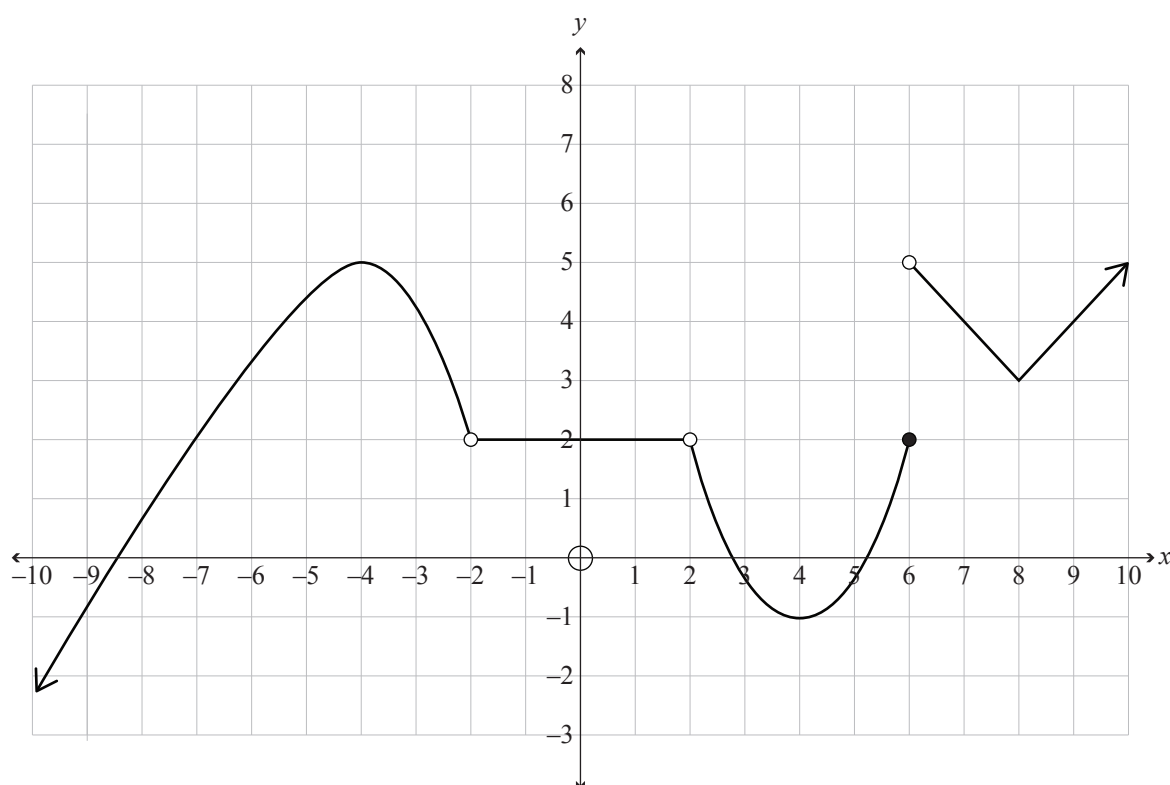


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- (b) The graph below shows the function  $y = f(x)$ .



For the function above:

- (i) Find the value(s) of  $x$  where  $f(x)$  is continuous but not differentiable.

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- (ii) Find the value(s) of  $x$  where  $f'(x) = 0$  and  $f''(x) < 0$  are both true.

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- (iii) What is the value of  $\lim_{x \rightarrow 6} f(x)$ ?

State clearly if the value does not exist.

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